

Question 1: Evaluate the following limits, if they exist. If a limit does not exist because it is $+\infty$ or $-\infty$, state which with an explanation of your reasoning. (Do not use L'Hospital's rule to evaluate limits.)

(a) $\lim_{x \rightarrow 2^-} \frac{x^2 + x - 6}{|x - 2|}$

[2]

(b) $\lim_{x \rightarrow -3^-} \frac{x + 2}{\sin(x + 3)}$

[2]

(c) $\lim_{x \rightarrow -\infty} \frac{x - 2x^5}{2x^2 + x^5}$

[3]

Question 2: Determine the value of k which makes the following function continuous at all real numbers:

$$f(x) = \begin{cases} x^2 & \text{if } x \leq -1 \\ k - x^3 & \text{if } x > -1 \end{cases}$$

[3]

Question 3:

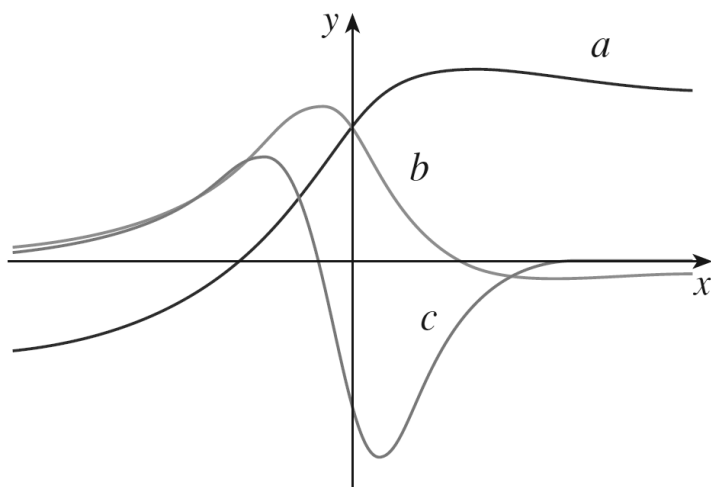
(a) Use the limit definition of the derivative to find $f'(x)$ if $f(x) = \frac{x}{x+1}$. Neatly show all steps and use proper notation. (No credit will be given if $f'(x)$ is found using derivative rules.)

[5]

(b) At what value(s) of x will f fail to be differentiable?

[2]

Question 4: The figure below shows the graphs of f , f' and f'' . Identify each by circling the appropriate label.



f is graph (circle one): a b c

f' is graph (circle one): a b c

f'' is graph (circle one): a b c

[3]

Question 5: Find the following derivatives (it is not necessary to simplify your answers, but marks will be deducted for improper use of notation):

(a) $f(x) = 4\sqrt{x} - \frac{5}{x}$

[2]

(b) $y = \sec(t)(1 - t^3)$

[3]

(c) $g(x) = \frac{\sin(x)}{1 + x - 3\cos(x)}$

[3]

(d) $y = \frac{t^2 \tan(t) - 1}{\pi^2}$

[2]

Question 6: Find the following derivatives (it is not necessary to simplify your answers, but marks will be deducted for improper use of notation):

(a) $y = (1 + x^{2/3})^{3/2}$

[2]

(b) $y = \frac{1}{2 + \sqrt{3t + 4}}$

[2]

(c) $g(x) = \tan(x \sin(x))$

[3]

(d) $y = \sqrt[5]{\frac{\csc(t)}{t}}$

[3]

Question 7: There are two tangent lines to the parabola $y = 2x^2$ that pass through the point $(0, -1)$ (sketch the parabola and tangent lines to see this.) For each of these tangent lines, determine the x -coordinate of the point where the line meet the parabola.

[5]

Question 8: Find an equation of the tangent line to the curve defined by $x + 2y + 1 = \frac{y^2}{x - 1}$ at the point $(x, y) = (2, -1)$.

[5]
