

1. Compute the following integrals. In some cases you must find a suitable parametrization for the given contour:

(a) $\int_{\gamma} (\operatorname{Im}(z))^2 dz$ where $\gamma(t) = 3t + 2it, -2 \leq t \leq 2$.

(b) $\int_{\gamma} \frac{z+1}{\bar{z}} dz$ where γ is the right half of the unit circle from $-i$ to i .

(c) $\int_{\gamma} |z|^2 dz$ where $\gamma(t) = t^2 + \frac{i}{t}, 1 \leq t \leq 2$.

(d) $\int_{\gamma} e^{\bar{z}} dz$ where γ consists of the line segment from $z = 0$ to $z = 2$ followed by the line segment from $z = 2$ to $z = 1 + \pi i$.

(e) $\int_{\gamma} \operatorname{Re}(z) dz$ where γ is the circle of radius 2 with positive orientation.

2. Compute the following integrals. Explain your reasoning, especially if relying on the path independence theorem.

(a) $\int_{\gamma} 2z dz$ where $\gamma(t) = 2 \cos^3(\pi t) - i \sin^2(\pi t/4), 0 \leq t \leq 2$.

(b) $\int_{\gamma} \frac{1}{z} dz$ where γ is the right half of the unit circle from $-i$ to i .

(c) $\int_{\gamma} \frac{1}{z} dz$ where γ is the left half of the unit circle from $-i$ to i .

(d) $\int_{\gamma} z \sin(z^2) dz$ where γ is the spiral $\gamma(t) = te^{it}, 0 \leq t \leq 8\pi$.