

(1) [2] Compute $h'(x)$ where $h(x) = \int_0^{x^2} \sqrt{1+r^3} dr$.

$$h'(x) = \sqrt{1+(x^2)^3} (2x)$$

$$= \boxed{\sqrt{1+x^6} (2x)}$$

(2) [3] Determine $\int x^2 e^{x^3} dx$.

$$\text{let } u = x^3$$

$$du = 3x^2 dx$$

$$\therefore \int x^2 e^{x^3} dx = \frac{1}{3} \int e^u du$$

$$= \frac{1}{3} e^u + C$$

$$= \boxed{\frac{1}{3} e^{x^3} + C}$$

(3) [5] Evaluate $\int_0^{\pi/2} \cos(x) \sin(\sin(x)) dx$.

$$\text{Let } \left. \begin{array}{l} u = \sin(x) \\ du = \cos(x) dx \end{array} \right\} \begin{array}{l} x=0 \Rightarrow u=0 \\ x=\frac{\pi}{2} \Rightarrow u = \sin(\frac{\pi}{2})=1 \end{array}$$

$$\therefore I = \int_0^1 \sin(u) du$$

$$= -\cos(u) \Big|_0^1$$

$$= -\cos(1) - (-\cos(0))$$

$$= \boxed{1 - \cos(1)}$$

(4) [5] Determine $\int t^5 \ln t dt$.

$$u = \ln(t) \quad dv = t^5 dt$$

$$du = \frac{1}{t} dt \quad v = \frac{t^6}{6}$$

$$I = \int u dv = uv - \int v du$$

$$= \frac{t^6 \ln(t)}{6} - \int \frac{t^6}{6} \frac{1}{t} dt$$

$$= \frac{t^6 \ln(t)}{6} - \frac{1}{6} \int t^5 dt$$

$$= \boxed{\frac{t^6 \ln(t)}{6} - \frac{1}{36} t^6 + C}$$