

Question 1:

(a)[3] Determine $\lim_{x \rightarrow -\infty} \arctan(x^2)$.

(b)[3] Determine $\cos^{-1}(-\sqrt{3}/2)$.

(c)[4] Let $f(x) = x \arcsin(x) + \sqrt{1-x^2}$. Determine $f'(1/2)$.

Question 2:

(a)[3] Evaluate the limit if it exists: $\lim_{x \rightarrow 0} \frac{\tanh(3x)}{\sinh(5x)}$.

(b)[3] Determine $f'(0)$ if $f(x) = \ln(\cosh(2x)) - \operatorname{sech}(\ln(1+x))$.

(c)[4] Does the equation $\sinh(x) = \cosh(x)$ have solutions? If so, find them. If not, explain why.

Question 3:

(a)[5] Evaluate the limit if it exists: $\lim_{x \rightarrow 0} \frac{x - \sin(x)}{\sin(x^2)}$

(b)[5] Evaluate the limit if it exists: $\lim_{x \rightarrow 0} \frac{\sqrt{1+x} - 1 - x/2}{x^2}$

Question 4:

(a)[5] Evaluate the limit if it exists: $\lim_{x \rightarrow 0^+} x(\ln(x))^2$

(b)[5] Evaluate the limit if it exists: $\lim_{x \rightarrow \infty} x^{(e^{-x})}$

Question 5: Use the definition of the definite integral in the form

$$\int_a^b f(x) dx = \lim_{n \rightarrow \infty} \sum_{i=1}^n f(x_i) \Delta x$$

to evaluate

$$\int_{-1}^2 3x^2 dx$$

Carefully set up the Riemann sum and clearly show the steps of your simplification.