

- (1) [3] Determine an equation of the tangent line to $y = x + \sqrt{x}$ at the point $(1, 2)$.

$$y' = 1 + \frac{1}{2}x^{-\frac{1}{2}}$$

$$y' \Big|_{x=1} = 1 + \frac{1}{2} = \frac{3}{2}$$

$$\therefore y - 2 = \frac{3}{2}(x - 1)$$

- (2) [3] Differentiate $y = t^4 - \frac{1}{\sqrt[4]{t^3}} = t^4 - t^{-\frac{3}{4}}$

$$y' = 4t^3 + \frac{3}{4}t^{-\frac{7}{4}}$$

(3) [3] Differentiate $y = \frac{x^2}{\sin(x)}$

$$y' = \frac{\sin(x)(2x) - x^2 \cos(x)}{\sin^2(x)}$$

(4) [3] Differentiate $g(x) = x^3 \cos(x)$

$$\begin{aligned} g'(x) &= 3x^2 \cos(x) + x^3 (-\sin(x)) \\ &= 3x^2 \cos(x) - x^3 \sin(x) \end{aligned}$$

(5) [3] Differentiate $f(\theta) = \frac{\sec(\theta)}{1 + \sec(\theta)}$

$$\begin{aligned} f'(\theta) &= \frac{[1 + \sec(\theta)] [\sec(\theta) \tan(\theta)] - \sec(\theta) [\sec(\theta) \tan(\theta)]}{[1 + \sec(\theta)]^2} \\ &= \frac{\sec(\theta) \tan(\theta)}{[1 + \sec(\theta)]^2} \end{aligned}$$