## **1** Exponentials

General Base $a > 0$	Special Case: Base $e = 2.71828 \cdots$
$a^b a^c = a^{b+c}$	$e^b e^c = e^{b+c}$
$\frac{a^b}{a^c} = a^{b-c}$	$\frac{e^b}{e^c}=e^{b-c}$
$(a^b)^c = a^{bc}$	$(e^b)^c=e^{bc}$
$\frac{d}{dx}\left[a^{x}\right]=a^{x}\ln\left(a\right)$	$\frac{d}{dx}\left[e^{x}\right]=e^{x}$

Derivative:

Laws:

## 2 Logarithms

**Definiton:**  $\log_a(b)$  is the power to which a is raised to give b.

**Definiton:**  $\ln(b) = \log_e(b)$ , the power to which *e* is raised to give *b*.

General Base a > 0

 $\log_a(bc) = \log_a(b) + \log_a(c)$ 

Special Case: Base  $e = 2.71828 \cdots$ 

 $\ln(bc) = \ln(b) + \ln(c)$ 

Laws:

$$\log_{a}\left(\frac{b}{c}\right) = \log_{a}(b) - \log_{a}(c) \qquad \qquad \ln\left(\frac{b}{c}\right) = \ln(b) - \ln(c)$$
$$\log_{a}(b^{c}) = c\log_{a}(b) \qquad \qquad \qquad \ln(b^{c}) = c\ln(b)$$

Change of Base: 
$$\log_b(c) = \frac{\log_a(c)}{\log_a(b)}$$
  $\log_b(c) = \frac{\ln(c)}{\ln(b)}$ 

**Derivative:** 
$$\frac{d}{dx} [\log_a(x)] = \frac{1}{x \ln(a)}$$
  $\frac{d}{dx} [\ln(x)] = \frac{1}{x}$ 

## **3** Inverse Properties

General Base 
$$a > 0$$
Special Case: Base  $e = 2.71828 \cdots$  $a^{\log_a(x)} = x$  $e^{\ln (x)} = x$  $\log_a(a^x) = x$  $\ln (e^x) = x$