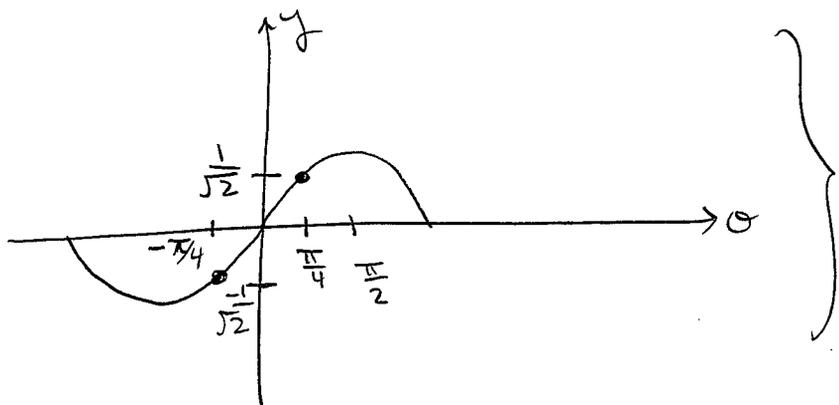


(1) [5] Determine the exact value of  $\arcsin(-1/\sqrt{2})$ .

$$\arcsin\left(-\frac{1}{\sqrt{2}}\right) = \text{angle } \theta \text{ in } \left[-\frac{\pi}{2}, \frac{\pi}{2}\right]$$

$$\text{such that } \sin(\theta) = -\frac{1}{\sqrt{2}}$$

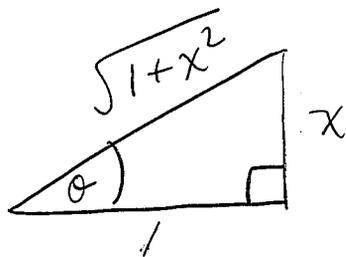


$$\therefore \theta = -\frac{\pi}{4}$$

$$\therefore \arcsin\left(-\frac{1}{\sqrt{2}}\right) = \boxed{-\frac{\pi}{4}}$$

(2) [5] Simplify  $\cos(\tan^{-1}x)$ . Your final simplified answer should not contain any trigonometric or inverse trigonometric functions.

$$\text{Let } \theta = \tan^{-1}x, \text{ so } \tan \theta = \frac{x}{1}$$



$$\therefore \cos(\tan^{-1}(x)) = \cos \theta$$

$$= \boxed{\frac{1}{\sqrt{1+x^2}}}$$

(3) [5] Differentiate

$$g(x) = \arccos(2 - 3x)$$

and state the domain of  $g(x)$ .

$$\begin{aligned} g'(x) &= \frac{-1}{\sqrt{1 - (2 - 3x)^2}} \cdot (-3) \\ &= \frac{3}{\sqrt{1 - (2 - 3x)^2}} \end{aligned}$$

Domain of  $g(x)$ : Must have

$$-1 \leq 2 - 3x \leq 1$$

$$\Rightarrow -3 \leq -3x \leq -1$$

$$\Rightarrow \frac{1}{3} \leq x \leq 1$$

$\therefore$  domain is  $[\frac{1}{3}, 1]$