

(1) [5 points] Let $f(x) = 4 + 3x - x^2$. Find and simplify $\frac{f(3+h) - f(3)}{h}$.

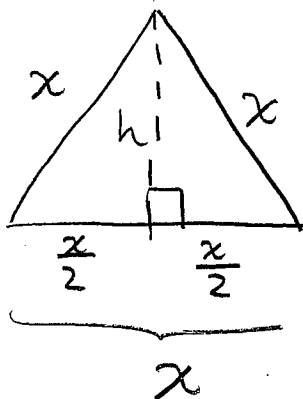
$$\begin{aligned} & \frac{f(3+h) - f(3)}{h} \\ &= \frac{[4 + 3(3+h) - (3+h)^2] - [4 + 3(3) - 3^2]}{h} \\ &= \frac{4 + 9 + 3h - 9 - 6h - h^2 - 4 - 9 + 9}{h} \\ &= \frac{-3h - h^2}{h} \\ &= -3 - h \end{aligned}$$

(2) [5 points] Let $f(x) = x + \frac{1}{x}$ and $g(x) = \frac{x+1}{x+2}$. Find $(f \circ g)(x)$ and state the domain.

$$\begin{aligned} (f \circ g)(x) &= f(g(x)) \\ &= \frac{x+1}{x+2} + \frac{1}{\left(\frac{x+1}{x+2}\right)} \\ &= \frac{x+1}{x+2} + \frac{x+2}{x+1} \\ &= \frac{x^2 + 2x + 1 + x^2 + 4x + 4}{(x+1)(x+2)} \\ &= \frac{2x^2 + 6x + 5}{(x+1)(x+2)} \end{aligned}$$

Using *, must have
 $x+2 \neq 0 \quad \& \quad \frac{x+1}{x+2} \neq 0$
 $\therefore x \neq -2, \quad x \neq -1$
 \therefore domain of $f \circ g$ is
 $\{x \mid x \neq -2, x \neq -1\}$,
or
 $(-\infty, -2) \cup (-2, -1) \cup (-1, \infty)$.

(3) [5 points] An equilateral triangle has side length x . Express the area of the triangle as a function of the side length.



$$A = \frac{1}{2} x h$$

Using Pythagoras' Theorem,

$$h^2 + \left(\frac{x}{2}\right)^2 = x^2,$$

$$\therefore h = \sqrt{x^2 - \frac{x^2}{4}}$$

$$= \sqrt{\frac{3x^2}{4}}$$

$$= \frac{\sqrt{3}}{2} x$$

$$\therefore A = \frac{1}{2} x \left(\frac{\sqrt{3}}{2} x\right)$$

$$= \frac{\sqrt{3}}{4} x^2.$$