

$$z = x^2 + y^2(1-x)^3:$$

local minimum of  $f(0,0)=0$  at the single critical point at  $(0,0)$ ,  
yet no absolute minimum or maximum exists

