**Question 1:** The following function has domain  $[0, \infty)$ :

$$f(x) = \begin{cases} \frac{\sqrt{x}-2}{x-4} & \text{if } x \neq 4\\ c & \text{if } x = 4 \end{cases}$$

Determine the value of c so that f is continuous at x = 4.

[5]

**Question 2:** Use the Intermediate Value Theorem to show that the equation sin(x) = 3 - 2x has a solution on the interval  $[0, 2\pi]$ .

[5]

**Question 3:** Evaluate the following limits, if they exist. If a limit does not exist because it is  $+\infty$  or  $-\infty$ , state which with an explanation of your reasoning. (Do not use L'Hospital's rule to evaluate limits.)

(a) 
$$\lim_{x \to -\infty} \frac{6x^5 - 7x^3 - 5}{7x^6 - 6x^5 + 5}$$

**(b)**  $\lim_{x \to 2^+} \frac{\cos(\pi x)}{2-x}$ 

[3]

(c)  $\lim_{x\to 1} \frac{2-x}{(x-1)^3}$ 

## Question 4:

(a) Use the limit definition of the derivative to find f'(x) if  $f(x) = \frac{5}{x+7}$ . Neatly show all steps and use proper notation. (No credit will be given if f'(x) is found using derivative rules.)

(b) Now check your work in part (a) by finding  $\frac{d}{dx} \left[ \frac{5}{x+7} \right]$  using derivative rules.

[8]

**Question 5:** Find the following derivatives (it is not necessary to simplify your answers, but marks will be deducted for improper use of notation):

(a) 
$$f(x) = 3\sqrt{x} - \frac{2}{3x} + \pi^2$$

**(b)** 
$$y = (t^3 - 3\cos(t))(2t - \sqrt{\pi})$$

(c) 
$$g(x) = \frac{x^2 - \sqrt[3]{x}}{\tan(x)}$$

(d) 
$$y = \frac{\sin(\theta)}{2} - \frac{2}{\sin(\theta)}$$

[2]

[3]

[3]

**Question 6:** The position of a particle along a straight line at time t is given by

$$s(t)=\frac{t^3}{3}+qt(t+1)$$

where q is a constant. At time t = 1 the velocity and acceleration are the same. Determine the value of the constant q.

**Question 7:** Find an equation of the tangent line to  $y = \frac{\pi^2 \cos(x)}{x}$  at the point where  $x = \pi$ .