

**Question 1:**

(a) Give the equation of the plane through the point  $(-3, 4, 7)$  that is parallel to the  $xy$ -plane.

[2]

(b) The point  $(a, a, a)$  is located in the first octant (where  $x \geq 0$ ,  $y \geq 0$  and  $z \geq 0$ ) at a distance 5 from the origin. Find the equation of the sphere of largest diameter that is located in the first octant and has  $(a, a, a)$  as the center.

[3]

(c) Find an equation for the set of all points  $(x, y, z)$  that are equidistant from the points  $(0, 0, 2)$  and  $(1, 1, 1)$ . Simplify your equation as much as possible.

[5]

Question 2: For this question use the vectors

$$\mathbf{a} = 2\mathbf{i} - \mathbf{j} + 3\mathbf{k}, \quad \mathbf{b} = 3\mathbf{i} - 2\mathbf{j} + \mathbf{k} \quad \text{and} \quad \mathbf{c} = \mathbf{i} + \mathbf{j} + \mathbf{k}$$

(a) Compute  $|\mathbf{a} - 3\mathbf{c}|$ .

[2]

(b) Compute  $|\mathbf{a} \times \mathbf{b}|$ .

[2]

(c) Compute  $\text{proj}_{\mathbf{a}}\mathbf{b}$ .

[3]

(d) Find a vector of magnitude 5 that is parallel to  $\mathbf{b}$  but pointing in the opposite direction.

[3]

**Question 3:** Determine all values of  $x$  for which  $\langle 3, 2, x \rangle$  and  $\langle 2x, 4, x \rangle$  are orthogonal.

[5]

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**Question 4:** Find orthogonal vectors  $\mathbf{a}$  and  $\mathbf{b}$  such that  $\mathbf{a}$  is parallel to  $\langle 1, 1, 1 \rangle$  and  $\mathbf{a} + \mathbf{b} = \langle 1, -2, 4 \rangle$ .

[5]

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**Question 5:** Find all values of  $x$  such that the angle between  $\langle 2, 1, -1 \rangle$  and  $\langle 1, x, 0 \rangle$  is  $\pi/4$ .

[5]

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**Question 6:** Find a unit normal vector to the plane containing the points  $P(1, -3, -2)$ ,  $Q(2, 0, -4)$  and  $R(6, -2, -5)$ .

[5]

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**Question 7:**

(a) Find the area of the triangle having vertices the points  $P(1, -3, -2)$ ,  $Q(2, 0, -4)$  and  $R(6, -2, -5)$ .

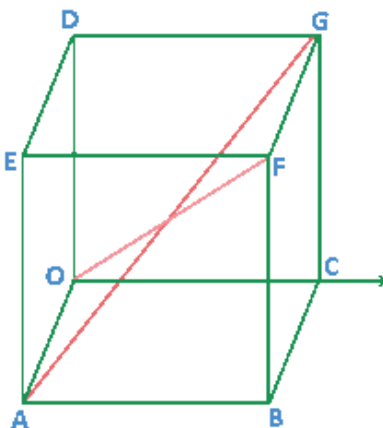
[2]

(b) Is the triangle in part (a) a right triangle?

[3]

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**Question 8:** Find the acute angle between the two diagonals  $OF$  and  $AG$  of a cube. If giving a decimal answer, round your final answer to one decimal place.



[5]