

**Question 1:**

- (a) Determine the linear approximation  $T_1(x)$  for  $f(x) = e^{-x} + e^{-2x}$  at  $a = 0$  and use it to approximate  $f(0.2)$ . Simplify your final answer.

**[5]**

- (b) Give an error bound on your approximation in part (a). Again, simplify your final answer.

**[5]**

**Question 2:**

(a) Use a Taylor polynomial of degree 2 to approximate  $1/1.1$ . Simplify your final answer.

[5]

(b) Give an error bound on your approximation in part (a). Again, simplify your final answer.

[5]

**Question 3:**

Find the Taylor series about  $a = -2$  for  $f(x) = 1 + x + 2x^2 + 3x^3$ . You should be able to write all terms of the series.

[5]

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**Question 4:** Find the first four nonzero terms of the Taylor series about  $a = 1$  for  $g(x) = \frac{3}{2 + 4x}$  and state the open interval of convergence.

[5]

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**Question 5:** Find the Maclaurin polynomial of degree 7 for  $f(x) = \frac{\ln(1+x^2)}{x}$ .

[3]

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**Question 6:** Find the sum of the infinite series  $1 - \frac{\pi^2}{2!} + \frac{\pi^4}{4!} - \dots$ .

[3]

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**Question 7:** Find the first three non-zero terms of the Maclaurin series for  $f(x) = e^{-x} \ln(1+x)$ .

[4]

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**Question 8:** Use series to find the limit:  $\lim_{x \rightarrow 0} \frac{\sin x - x + \frac{x^3}{6}}{x^5}$

[5]

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**Question 9:** It can be shown that

$$\cos[\sin(x)] = 1 - \frac{x^2}{2} + \frac{5x^4}{24} - \frac{37x^6}{720} + \dots$$

for all real numbers  $x$ . Use this fact to find the first 3 non-zero terms of the Maclaurin series for  $g(x) = \sin[\sin(x^2)] \cos(x^2)$ .

[5]

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