## 1 **Exponentials**

General Base $a > 0$	Special Case: Base $e = 2.71828 \cdots$
$a^b a^c = a^{b+c}$	$e^b e^c = e^{b+c}$
$\frac{a^b}{a^c} = a^{b-c}$	$\frac{e^b}{e^c} = e^{b-c}$
$(a^b)^c = a^{bc}$	$(e^b)^c = e^{bc}$
$\frac{d}{dx}\left[a^{x}\right] = a^{x}\ln\left(a\right)$	$\frac{d}{dx}\left[e^x\right] = e^x$

**Derivative:** 

Laws:

## 2 Logarithms

**Definiton:**  $\log_a(b)$  is the power to which a is raised to give b.

**Definiton:**  $\ln(b) = \log_e(b)$ , the power to which e is raised to give b.

General Base a > 0

Laws:

3

Laws:  

$$\log_a(bc) = \log_a(b) + \log_a(c) \qquad \ln(bc) = \ln(b) + \ln(c)$$

$$\log_a\left(\frac{b}{c}\right) = \log_a(b) - \log_a(c) \qquad \ln\left(\frac{b}{c}\right) = \ln(b) - \ln(c)$$

$$\log_a(b^c) = c\log_a(b) \qquad \ln(b^c) = c\ln(b)$$
Change of Base:  

$$\log_b(c) = \frac{\log_a(c)}{\log_a(b)} \qquad \log_b(c) = \frac{\ln(c)}{\ln(b)}$$

Special Case: Base  $e = 2.71828 \cdots$ 

**Derivative:** 
$$\frac{d}{dx} \left[ \log_a(x) \right] = \frac{1}{x \ln(a)}$$
  $\frac{d}{dx} \left[ \ln(x) \right] = \frac{1}{x}$ 

**Inverse Properties**