

1. Compute the following integrals. In some cases you must find a suitable parametrization for the given contour:

(a)  $\int_{\gamma} (\operatorname{Im}(z))^2 dz$  where  $\gamma$  is parametrized by  $z(t) = 3t + 2it, -2 \leq t \leq 2$ .

(b)  $\int_{\gamma} \frac{z+1}{\bar{z}} dz$  where  $\gamma$  is the right half of the unit circle from  $-i$  to  $i$ .

(c)  $\int_{\gamma} |z|^2 dz$  where  $\gamma$  is  $z(t) = t^2 + \frac{i}{t}, 1 \leq t \leq 2$ .

(d)  $\int_{\gamma} e^{\bar{z}} dz$  where  $\gamma$  consists of the line segment from  $z = 0$  to  $z = 2$  followed by the line segment from  $z = 2$  to  $z = 1 + \pi i$ .

(e)  $\int_{\gamma} \operatorname{Re}(z) dz$  where  $\gamma$  is the circle of radius 2 with positive orientation.

2. Compute the following integrals. Explain your reasoning, especially if relying on the path independence theorem.

(a)  $\int_{\gamma} 2z dz$  where  $\gamma$  is parametrized by  $z(t) = 2 \cos^3(\pi t) - i \sin^2(\pi t/4), 0 \leq t \leq 2$ .

(b)  $\int_{\gamma} \frac{1}{z} dz$  where  $\gamma$  is the right half of the unit circle from  $-i$  to  $i$ .

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(d)  $\int_{\gamma} z \sin(z^2) dz$  where  $\gamma$  is the spiral  $z(t) = te^{it}, 0 \leq t \leq 8\pi$ .

(e)  $\int_{\gamma} \operatorname{Log}(z) dz$  where  $\gamma$  is the unit circle. (Harder: be careful with the branch cut.)