

Question 1: Compute $\iint_R xy\sqrt{x^2 + y^2} dA$ where $R = [0, 1] \times [0, 1]$.

[5]

Question 2: Calculate $\int_0^2 \int_{x^2}^4 x^3 e^{y^3} dy dx$ (reversing the order of integration may help here.)

[5]

Question 3: Determine the volume of the solid that lies under the plane $x + 2y - z = 0$ and above the region in the xy -plane bounded by $y = x$ and $y = x^2$.

[5]

Question 4: Determine the volume of the solid in the first octant that lies between the paraboloid $z = 1 + x^2 + y^2$ and the plane $z = 10$. (Polar coordinates may be helpful here.)

[5]

Question 5: Evaluate $\iiint_E x \, dV$ where E is the solid tetrahedron with vertices $(0, 0, 0)$, $(2, 0, 0)$, $(0, 1, 0)$ and $(0, 0, 4)$

Question 6: Evaluate $\iiint_E xy^2$ where E is the solid in the first octant that is bounded by the cylinders $x^2 + y^2 = 1$ and $x^2 + y^2 = 4$, and on top by the plane $y + z = 3$.

Question 7: Express the integral

$$\int_{-1}^1 \int_{x^2}^1 \int_0^{1-y} f(x, y, z) \, dz \, dy \, dx$$

as an iterated integral in the order $dx \, dy \, dz$