

1. Determine the radius of convergence of  $\sum_{n=1}^{\infty} \frac{(z+1)^n}{(n+5)^3 3^n}$ .
2. Determine the sum of the series  $\sum_{n=1}^{\infty} n^2 z^n$  for  $|z| < 1$ . (Hint: start with the series for  $1/(1-z)$ .)
3. Determine the radius of convergence of the Taylor series for
  - (a)  $\frac{\sin z}{z^2 + 4}$  about  $z = 0$ .
  - (b)  $\frac{e^z}{z^2 - z}$  about  $z = 4i$ .
4. Determine the Taylor series for  $f(z) = \sinh(z) \cosh(z)$  about  $z = 0$  and state the radius of convergence.
5. Find a Laurent series expansion of  $\frac{3z-3}{(2z-1)(z-2)}$  on  $1/2 < |z-1| < 1$ .
6. Find a Laurent series expansion of  $\frac{e^{(z^2)}}{z^3}$  about  $z = 0$ .