

(1) [5] Solve for y :

$$\sqrt{y} + \sqrt{y+2} = 3$$

$$(\sqrt{y} + \sqrt{y+2})^2 = 3^2$$

$$y + 2\sqrt{y}\sqrt{y+2} + y+2 = 9$$

$$(2\sqrt{y}\sqrt{y+2})^2 = (7-2y)^2$$

$$4y(y+2) = 49 - 28y + 4y^2$$

$$\cancel{4y^2} + 8y = 49 - 28y + \cancel{4y^2}$$

$$36y = 49$$

$$\boxed{y = \frac{49}{36}}$$

(2) [5] Solve for n :

$$4 + n^2 = 2n$$

$$n^2 - 2n + 4 = 0$$

$$n = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

$$= \frac{-(-2) \pm \sqrt{(-2)^2 - 4(1)(4)}}{2(1)}$$

$$= \frac{2 \pm \sqrt{-12}}{2} \left\{ \begin{array}{l} \text{no real} \\ \text{solutions.} \end{array} \right.$$

(3) [5] Solve for x:

$$\frac{2}{x^2-1} - \frac{1}{x(x-1)} = \frac{2}{x^2}$$

$$\frac{2}{(x-1)(x+1)} - \frac{1}{x(x-1)} = \frac{2}{x^2} \quad \left. \begin{array}{l} \text{notice:} \\ x \neq 0, \\ x \neq 1, \\ x \neq -1 \end{array} \right\}$$

multiply through by $x^2(x-1)(x+1)$:

$$2x^2 - x(x+1) = 2(x-1)(x+1)$$

$$\cancel{2x^2} - x^2 - x = \cancel{2x^2} - 2$$

$$x^2 + x - 2 = 0$$

$$x = \frac{-1 \pm \sqrt{1^2 - 4(1)(-2)}}{2(1)}$$

$$= \frac{-1 \pm \sqrt{9}}{2}$$

$$= \frac{-1 \pm 3}{2}$$

$$\therefore \boxed{\cancel{x=1}}, \quad \boxed{x=-2}$$

↑
extraneous
root