

(1) [6] The equation of motion of a particle is  $s(t) = t^3 - 3t$ , where  $s$  is in meters and  $t$  is in seconds. Determine the acceleration of the particle when the velocity is zero.

$$s(t) = t^3 - 3t$$

$$v(t) = s'(t) = 3t^2 - 3$$

$$a(t) = v'(t) = 6t$$

velocity is zero  $\Rightarrow v(t) = 0$

$$\Rightarrow 3t^2 - 3 = 0$$

$$\therefore t^2 = 1$$

$$t = 1$$

$$\therefore a(1) = (6)(1) = \boxed{6 \frac{m}{s^2}}$$

(2) [3] Differentiate

$$f(x) = x - 3 \sin x$$

$$f'(x) = 1 - 3 \cos x$$

(3) [3] Differentiate.

$$y = \frac{r^2}{1 + \sqrt{r}} = \frac{r^2}{1 + r^{1/2}}$$

$$y' = \frac{(1 + r^{1/2})(2r) - (r^2)(\frac{1}{2}r^{-1/2})}{(1 + r^{1/2})^2}$$

(4) [3] Differentiate

$$y = t^3 \cos t$$

$$y' = 3t^2 \cos t - t^3 \sin t$$