

(1) [5] Let

$$A = \begin{bmatrix} 1 & -2 & 0 \\ 5 & 1 & 2 \end{bmatrix}, \quad B = \begin{bmatrix} 2 & -3 & 4 \\ 0 & 2 & 1 \end{bmatrix}, \quad C = \begin{bmatrix} -3 & 0 & 5 \\ 2 & 1 & 3 \end{bmatrix}$$

Compute $3A + 4(B + C)$.

$$\begin{aligned} & 3 \begin{bmatrix} 1 & -2 & 0 \\ 5 & 1 & 2 \end{bmatrix} + 4 \left(\begin{bmatrix} 2 & -3 & 4 \\ 0 & 2 & 1 \end{bmatrix} + \begin{bmatrix} -3 & 0 & 5 \\ 2 & 1 & 3 \end{bmatrix} \right) \\ &= \begin{bmatrix} 3 & -6 & 0 \\ 15 & 3 & 6 \end{bmatrix} + 4 \begin{bmatrix} -1 & -3 & 9 \\ 2 & 3 & 4 \end{bmatrix} \\ &= \begin{bmatrix} 3 & -6 & 0 \\ 15 & 3 & 6 \end{bmatrix} + \begin{bmatrix} -4 & -12 & 36 \\ 8 & 12 & 16 \end{bmatrix} \\ &= \begin{bmatrix} -1 & -18 & 36 \\ 23 & 15 & 22 \end{bmatrix} \end{aligned}$$

(2) [5] Compute the following product:

$$\begin{aligned} & \begin{bmatrix} 1 & -1 & 6 \\ 2 & 0 & -1 \\ 3 & 1 & 2 \end{bmatrix} \begin{bmatrix} 3 & 2 \\ 0 & 1 \\ 1 & 0 \end{bmatrix} \\ &= \begin{bmatrix} 9 & 1 \\ 5 & 4 \\ 11 & 7 \end{bmatrix} \end{aligned}$$

(3) [5] Let $A = \begin{bmatrix} 3 & 7 \\ 2 & 5 \end{bmatrix}$. Determine A^{-1} .

$$\left[\begin{array}{cc|cc} 3 & 7 & 1 & 0 \\ 2 & 5 & 0 & 1 \end{array} \right]$$

$$r_1 \leftrightarrow r_2: \left[\begin{array}{cc|cc} 2 & 5 & 0 & 1 \\ 3 & 7 & 1 & 0 \end{array} \right]$$

$$R_1 = \frac{1}{2}r_1: \left[\begin{array}{cc|cc} 1 & \frac{5}{2} & 0 & \frac{1}{2} \\ 3 & 7 & 1 & 0 \end{array} \right]$$

$$R_2 = -3r_1 + r_2: \left[\begin{array}{cc|cc} 1 & \frac{5}{2} & 0 & \frac{1}{2} \\ 0 & -\frac{1}{2} & 1 & -\frac{3}{2} \end{array} \right]$$

$$R_2 = -2r_2: \left[\begin{array}{cc|cc} 1 & \frac{5}{2} & 0 & \frac{1}{2} \\ 0 & 1 & -2 & 3 \end{array} \right]$$

$$R_1 = \left(-\frac{5}{2}\right)r_2 + r_1: \left[\begin{array}{cc|cc} 1 & 0 & 5 & -7 \\ 0 & 1 & -2 & 3 \end{array} \right]$$

$$\therefore A^{-1} = \begin{bmatrix} 5 & -7 \\ -2 & 3 \end{bmatrix}$$