

(1) [3 points] Find the derivative of $H(t) = \tanh(e^t)$.

$$H'(t) = \operatorname{sech}^2(e^t) \cdot e^t$$

(2) [3 points] Find the derivative of $y = e^{\cosh(7x)}$.

$$y' = e^{\cosh(7x)} \cdot \sinh(7x) \cdot 7$$

(3) [5 points] Find the limit: $\lim_{x \rightarrow 1} \frac{1-x+\ln x}{1+\cos(\pi x)}$ $\rightarrow \frac{0}{0}$

$$\stackrel{H}{=} \lim_{x \rightarrow 1} \frac{-1 + \frac{1}{x}}{-\pi \sin(\pi x)} \rightarrow \frac{0}{0}$$

$$\stackrel{H}{=} \lim_{x \rightarrow 1} \frac{-\frac{1}{x^2}}{-\pi^2 \cos(\pi x)}$$

$$= \frac{\left(-\frac{1}{1}\right)}{\pi^2} = \boxed{\frac{-1}{\pi^2}}$$

(4) [4 points] Find f if $f'(x) = \sqrt{x}(6+5x)$ and $f(1) = 10$.

$$f'(x) = x^{1/2}(6+5x) = 6x^{1/2} + 5x^{3/2}$$

$$\therefore f(x) = 6 \frac{x^{3/2}}{(3/2)} + 5 \frac{x^{5/2}}{(5/2)} + C = 4x^{3/2} + 2x^{5/2} + C$$

$$f(1) = 10, \text{ so}$$

$$10 = 4(1)^{3/2} + 2(1)^{5/2} + C$$

$$\therefore C = 10 - 4 - 2 = 4$$

$$\therefore f(x) = 4x^{3/2} + 2x^{5/2} + 4.$$