

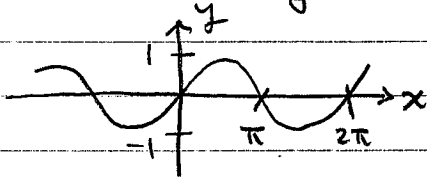
# SUMMARY OF INVERSE TRIG FUNCTIONS

①

$f(x) = \sin^{-1}(x)$  or  $\arcsin(x)$ .

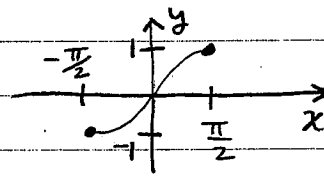
## Definition

① start with  $y = \sin x$



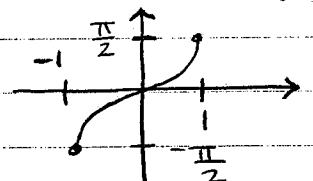
$y = \sin(x)$

② restrict domain



$y = \sin(x), -\frac{\pi}{2} \leq x \leq \frac{\pi}{2}$

③ reflect about  $y=x$



$y = \sin^{-1}(x)$ .

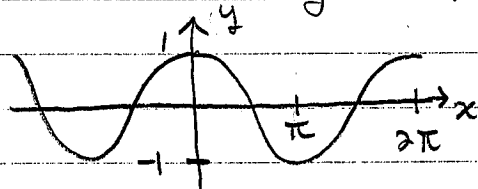
$\therefore f(x) = \sin^{-1}(x)$   
= angle  $y$  in  $[-\frac{\pi}{2}, \frac{\pi}{2}]$  such that  $\sin(y) = x$

$\frac{d}{dx} [\sin^{-1}(x)] = \frac{1}{\sqrt{1-x^2}}, -1 < x < 1$

$f(x) = \cos^{-1}(x)$  or  $\arccos(x)$ .

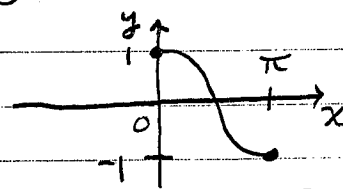
## Definition:

① start with  $y = \cos(x)$



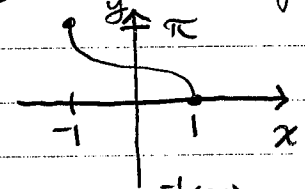
$y = \cos(x)$

② restrict domain



$y = \cos(x), 0 \leq x \leq \pi$

③ reflect about  $y=x$



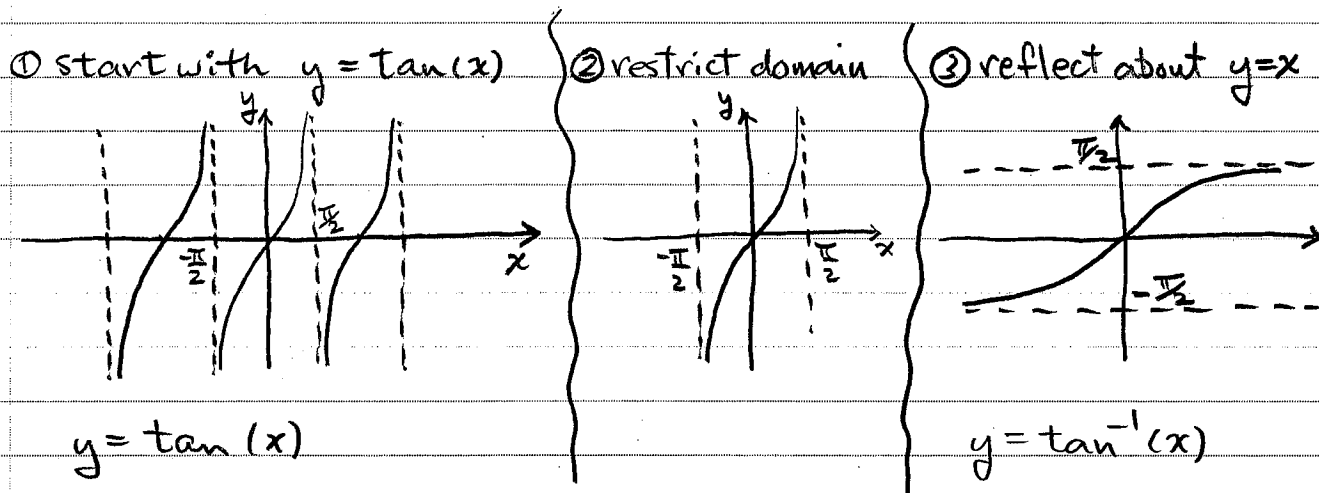
$y = \cos^{-1}(x)$

$\therefore f(x) = \cos^{-1}(x) =$  angle  $y$  in  $[0, \pi]$  such that  $\cos(y) = x$

$\frac{d}{dx} [\cos^{-1}(x)] = \frac{-1}{\sqrt{1-x^2}}, -1 < x < 1$

$f(x) = \tan^{-1}(x)$  or  $\arctan(x)$

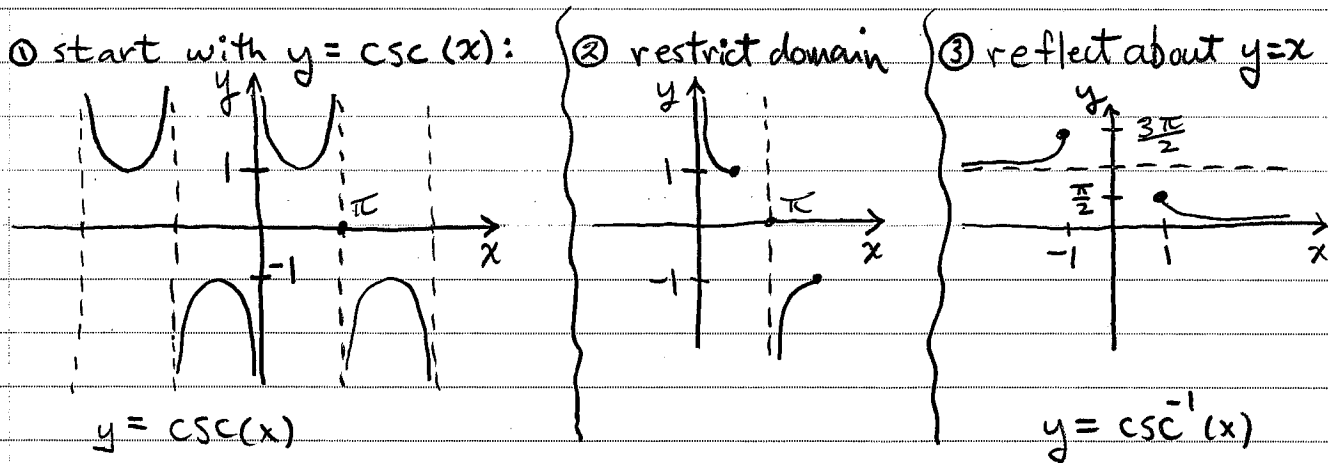
Definition:



$\therefore f(x) = \tan^{-1}(x) = \text{angle } y \text{ in } (-\frac{\pi}{2}, \frac{\pi}{2}) \text{ such that } \tan(y) = x$

$$\frac{d}{dx} [\tan^{-1}(x)] = \frac{1}{1+x^2}$$

$f(x) = \csc^{-1}(x)$  or  $\text{arccsc}(x)$

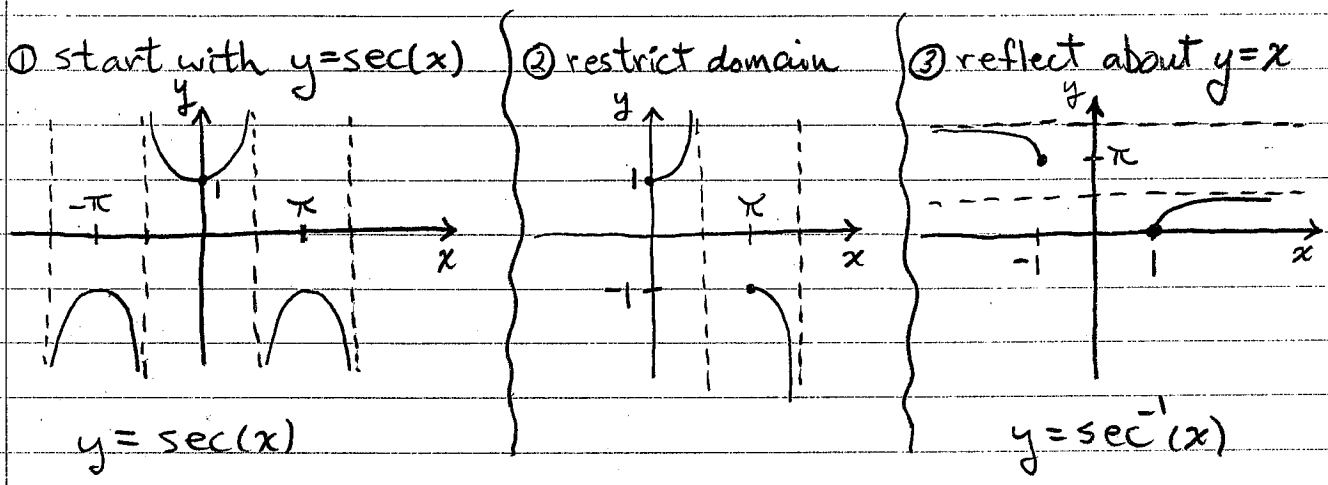


$\therefore f(x) = \csc^{-1}(x) = \text{angle } y \text{ in } (0, \frac{\pi}{2}] \cup (\pi, \frac{3\pi}{2}]$   
such that  $\csc(y) = x$ .

$$\frac{d}{dx} [\csc^{-1}(x)] = \frac{-1}{x\sqrt{x^2-1}}, \quad |x| > 1$$

$f(x) = \sec^{-1}(x)$  or  $\text{arcsec}(x)$

Definition :

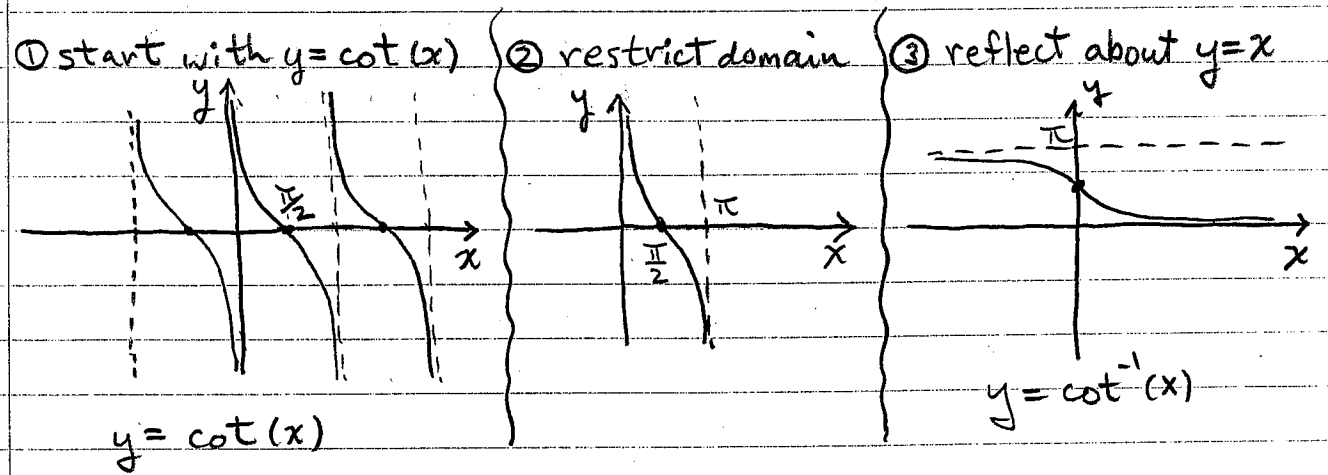


$\therefore f(x) = \sec^{-1}(x) = \text{angle } y \text{ in } [0, \frac{\pi}{2}) \cup [\pi, \frac{3\pi}{2})$   
such that  $\sec(y) = x$

$\frac{d}{dx} [\sec^{-1}(x)] = \frac{1}{x\sqrt{x^2-1}}, \quad |x| > 1$

$f(x) = \cot^{-1}(x)$  or  $\text{arccot}(x)$

Definition :



$\therefore f(x) = \cot^{-1}(x) = \text{angle } y \text{ in } (0, \pi)$  such that  $\cot(y) = x$

$\frac{d}{dx} [\cot^{-1}(x)] = \frac{-1}{1+x^2}$