

(1)[5 points] Find the equation of the line through $(-2, 4)$ and perpendicular to $3x + y - 5 = 0$.

$$3x + y - 5 = 0$$

$$y = -3x + 5 \quad \left. \vphantom{y = -3x + 5} \right\} \text{slope } m = -3$$

\therefore slope of line through $(-2, 4)$ is $\frac{-1}{-3} = \frac{1}{3}$

\therefore equation is $\boxed{y - 4 = \frac{1}{3}(x + 2)}$

$$\cong y = \frac{1}{3}x + \frac{2}{3} + 4$$

$$\boxed{y = \frac{1}{3}x + \frac{14}{3}}$$

(2)[5 points] Find the points of intersection of the graphs of the linear functions $f(x) = 4x + 7$ and $g(x) = \frac{1}{3}x + \frac{10}{3}$.

$$4x + 7 = \frac{1}{3}x + \frac{10}{3} \quad \left. \vphantom{4x + 7 = \frac{1}{3}x + \frac{10}{3}} \right\} \begin{array}{l} \text{multiplying} \\ \text{through by 3} \end{array}$$

$$12x + 21 = x + 10$$

$$11x = -11$$

$$x = -1$$

$$\therefore y = f(-1) = 4(-1) + 7 = 3$$

\therefore point of intersection is $(-1, 3)$

(3)[5 points] Put $f(x) = 4x^2 - 4x - 1$ into standard form, give the vertex and axis of symmetry, and sketch the graph of the function.

$$\begin{aligned} f(x) &= 4x^2 - 4x - 1 \\ &= 4 \left[x^2 - x - \frac{1}{4} \right] \\ &= 4 \left[\left(x - \frac{1}{2}\right)^2 - \frac{1}{4} - \frac{1}{4} \right] \\ &= 4 \left(x - \frac{1}{2}\right)^2 - 1 - 1 \\ &= 4 \left(x - \frac{1}{2}\right)^2 - 2 \end{aligned}$$

Vertex is $\left(\frac{1}{2}, -2\right)$

axis of symmetry is $x = \frac{1}{2}$

