MAR 22, 2019

HW # 6 (Due Mar 29)

- 1. Ex. 4.5 # 2(a) & (b) only, 8(i)(iii)(v)(vii), 15, 26(b).
- 2. Prove that if p and p + 2 are both primes with p > 3 then 6|p + 1 (use Division Algorithm and check all cases of 3q + r).
- 3. Prove that if 2^n-1 is prime then n is prime (by contrapositive). Hint: $x^k-y^k=(x-y)(x^{k-1}+x^{k-2}y+\cdots+x^2y^{k-3}+xy^{k-2}+y^{k-1})$
- 4. Prove that for any positive integer k, there exists a sequence of k consecutive composite numbers (by construction).
- 5. Prove that if a, b, c and m are integers such that $m \ge 2$, c > 0 and $a \equiv b \pmod{m}$ then $ac \equiv bc \pmod{m}$.
- 6. Ex. 14.3 # 32, 38(c)