

Ex 7.1

17/ If spinner 3 is spun once and then spinner 2 is spun twice then the sample space is ①

$$S = \{1AA, 1AB, 1AC, 1BA, 1BB, 1BC, 1CA, 1CB, 1CC, \\ 2AA, 2AB, 2AC, 2BA, 2BB, 2BC, 2CA, 2CB, 2CC, \\ 3AA, 3AB, 3AC, 3BA, 3BB, 3BC, 3CA, 3CB, 3CC, \\ 4AA, 4AB, 4AC, 4BA, 4BB, 4BC, 4CA, 4CB, 4CC\}$$

18/ Expt: Toss 2 dice and then a coin

$$n(S) = \left(\begin{array}{c} \text{no. of ways} \\ \text{to roll one die} \end{array} \right) \times \left(\begin{array}{c} \text{no. of ways to} \\ \text{roll one die} \end{array} \right) \times \left(\begin{array}{c} \text{no. of ways to} \\ \text{toss a coin} \end{array} \right) \\ = 6 \times 6 \times 2 \\ = \underline{\underline{72}}$$

24/ If the coin is known to be fair, assignment 1 should be used because all outcomes would be equally likely.

$$\begin{aligned} P(\overline{A \cup B}) &= 1 - P(A \cup B) \\ &= 1 - (0.35 + 0.60) \\ &= 0.05 \end{aligned}$$

36/ Let A be the event that material E is short
B " " " " F is short
then

$$\begin{aligned} P(\text{being short of either material}) &= P(A \cup B) \\ &= 0.06 + 0.04 - 0.02 \\ &= 0.08 \end{aligned}$$

38/ (a) $P(\text{at most 2 people in line})$
 $= P(\text{exactly 0 in line}) + P(\text{exactly 1 in line})$
 $\quad \quad \quad + P(\text{exactly 2 in line})$
 $= 0.10 + 0.15 + 0.20$
 $= 0.45$

(3)

Ex 7.3

14/

$P(\text{In a group of 6 people, at least 2 were born in the same month})$

$$= 1 - P(\text{no two were born in the same month})$$

$$= 1 - \frac{P(12, 6)}{12^6}$$

$$= 1 - \frac{665,280}{2,985,984}$$

$$= 1 - 0.2228$$

$$= 0.7772$$

$$= 0.7772$$

35/ Expt: Select 5 cards from a deck of 52 cards
 S = all possible combinations of 5 cards

(a) E = all combinations with 5 hearts

$$P(E) = \frac{C(13, 5)}{C(52, 5)} = \frac{\frac{13!}{5!8!}}{\frac{52!}{5!47!}} = \frac{1287}{2598960} \approx 0.000495$$

(b) E = all combinations with exactly 4 spades

$$P(E) = \frac{C(13, 4) \cdot C(39, 1)}{C(52, 5)} = \frac{715 \times 39}{2598960} \approx 0.0107$$

(c) E = all combinations with exactly 2 clubs

$$P(E) = \frac{C(13, 2) \cdot C(39, 3)}{C(52, 5)} = \frac{78 \times 9139}{2598960} \approx 0.2743$$

(4)

26/ Expt: 30 transformers are chosen at random from 50.
 S = all the different ways of choosing 30 transformers
 A = the event that all 30 are non-defective

$$\begin{aligned}
 P(A) &= \frac{C(A)}{C(S)} \\
 &= \frac{C(40, 30)}{C(50, 30)} \\
 &= \underline{\underline{0.000018}}
 \end{aligned}$$

38/ Expt: Assign 5 numbers (1 to 8) to the 5 passengers

S = all possible ways of assigning 5 floor numbers to 5 passengers

A = the event that no two passengers get assigned the same number

$$\begin{aligned}
 P(A) &= \frac{C(A)}{C(S)} && \text{because all simple events are equally likely} \\
 &= \frac{P(8, 5)}{8^5} \\
 &= \underline{\underline{0.2051}}
 \end{aligned}$$

(5)

Ex 7.4

$$\begin{aligned}
 P(D) &= P(A \cap D) + P(B \cap D) \\
 &= P(A) \cdot P(D|A) + P(B) \cdot P(D|B) \\
 &= (0.7)(0.1) + (0.3)(0.8) \\
 &= 0.07 + 0.24 \\
 &= \underline{0.31}
 \end{aligned}$$

$$12/ \quad P(E) = 0.6, \quad P(F) = 0.5, \quad P(E \cap F) = 0.3$$

$$P(F|E) = \frac{P(E \cap F)}{P(E)}$$

$$\begin{aligned}
 &= \frac{0.3}{0.6} \\
 &= \underline{0.50}
 \end{aligned}$$

$$P(E|F) = \frac{P(E \cap F)}{P(F)}$$

$$\begin{aligned}
 &= \frac{0.3}{0.5} \\
 &= \underline{0.60}
 \end{aligned}$$

38/ Expt: A card is drawn at random from a deck of 52 cards

$$\begin{aligned}
 (a) \quad P(\text{the card is a black jack}) &= \frac{2}{52} \\
 &= \underline{\underline{1/26}}
 \end{aligned}$$

$$\begin{aligned}
 (b) \quad P(\text{the card is a black jack} \mid \text{a jack was picked}) \\
 &= \frac{2}{4} \\
 &= \underline{\underline{1/2}}
 \end{aligned}$$

$$\begin{aligned}
 (c) \quad P(\text{the card is a black jack} \mid \text{a black card was picked}) \\
 &= \frac{2}{26} \\
 &= \underline{\underline{1/13}}
 \end{aligned}$$

Ex 7.4

$$\begin{aligned} 50\% \quad P(G \cap I) &= 0.32 \\ P(I) &= 0.76 \end{aligned}$$

$$\begin{aligned} P(G|I) &= \frac{P(G \cap I)}{P(I)} \\ &= \frac{0.32}{0.76} \\ &= \underline{\underline{0.4211}} \end{aligned}$$

$$38/ \quad (a) \quad P(\text{the card is a black jack}) = \frac{2}{52} = \underline{\underline{\frac{1}{26}}}$$

$$\begin{aligned} (b) \quad P(\text{the card is a black jack} \mid \text{the card is a jack}) \\ &= \frac{2}{4} \\ &= \underline{\underline{\frac{1}{2}}} \end{aligned}$$

$$\begin{aligned} (c) \quad P(\text{the card is a black jack} \mid \text{the card is a black card}) \\ &= \frac{2}{26} \\ &= \underline{\underline{\frac{1}{13}}} \end{aligned}$$

$$\begin{aligned} 45/ \quad P(1^{\text{st}} \text{ card is red and the second is black}) \\ &= P(1^{\text{st}} \text{ card is red}) \cdot P(2^{\text{nd}} \text{ is black} \mid 1^{\text{st}} \text{ is red}) \\ &= \frac{1}{2} \cdot \frac{26}{51} \\ &= \underline{\underline{\frac{13}{51}}} \end{aligned}$$

7

Ken

$$P(V|R) = ?$$

$$P(v) = \frac{5}{9}$$

$$p(v|\vec{R}) = 1$$

$$p(R) = \underline{3/4}$$

A probability tree diagram for a two-stage experiment. The first stage has two branches: R with probability $\frac{3}{4}$ and $\bar{R}$ with probability $\frac{1}{4}$. The second stage branches from R are V and $\bar{V}$, and from $\bar{R}$ are V and 0 .

$$P(V) = P(R_{AV}) + P(\bar{R}_{NV})$$

$$P(R \cap V) = \frac{5}{9} - \frac{1}{4}$$
$$= \frac{11}{36}$$

$$\begin{aligned} \therefore P(R|V) &= \frac{P(R \cap V)}{P(V)} \\ &= \frac{11/36}{5/9} \\ &= \frac{11}{20} \end{aligned}$$



$$P(C/T) = 0.35$$

$$P(C|T) = 0.40$$

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graph LR
    Root(( )) ---|0.70| T[T]
    Root ---|0.30| Tbar[T̄]
    T ---|0.85| TC[C]
    T ---|0.15| TCbar[C̄]
    Tbar ---|0.40| TbarC[C]
    Tbar ---|0.60| TbarCbar[C̄]
  
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$$\begin{aligned} P(\bar{T} \cap C) &= P(\bar{T}) \cdot P(C|\bar{T}) \\ &= 0.30 \times 0.40 \\ &= 0.12 \end{aligned}$$

$$\therefore P(C) = P(T \cap C) + P(\bar{T} \cap C)$$
$$= 0.595 + 0.12$$
$$= \underline{0.715} \quad \text{or} \quad \underline{71.5\%}$$