MORE ABOUT UNITS OF CONCENTRATION

There are a number of different ways of expressing solute concentration that are commonly used. Some of these are listed below.

Molarity, \( M \) = moles solute/liter of solution

Normality, \( N \) = equivalents of solute/liter of solution

Weight %, \( Wt \ % \) = (mass of solute/mass of solution) x 100%

Parts per million, \( ppm \) = (mass of solute/mass of solution) x \( 10^6 \)

Mass per volume, \( mg/L \) = mass of solute/liter of solution

molality, \( m \) = moles of solute/mass of solvent

mole fraction, \( \chi \) = moles of solute/total moles

Concentrations expressed as ppm and N are less familiar to most students at this stage.

Parts per million:
The number of milligrams of solute per kg of solution = one ppm, since 1 mg = \( 10^{-3} \) g and 1 kg = \( 10^3 \) g.

Assuming the density of water is 1.00 g/mL, 1 liter of solution = 1 kg and hence, 1 mg/L = 1 ppm. This is generally true for freshwater and other dilute aqueous solutions.

Parts per million concentrations are essentially mass ratios (solute to solution) x a million (\( 10^6 \)). In this sense, they are similar to wt %, which could be thought of as parts per hundred (although nobody uses this term).

Other variations on this theme include:

ppt – parts per thousand (used for common ions in sea water) also written as ‰

ppb – parts per billion (used for heavy metals and organics)

pptr – parts per trillion (used for trace metals and trace organics)

The following table summarizes common mass ratios for solutions and solids.

<table>
<thead>
<tr>
<th>Unit</th>
<th>Solutions</th>
<th></th>
<th>Solids</th>
</tr>
</thead>
<tbody>
<tr>
<td>ppm</td>
<td>mg/L</td>
<td>( \mu g/mL )</td>
<td>mg/kg</td>
</tr>
<tr>
<td>ppb</td>
<td>( \mu g/L )</td>
<td>ng/mL</td>
<td>( \mu g/kg )</td>
</tr>
<tr>
<td>pptr</td>
<td>ng/L</td>
<td>pg/mL</td>
<td>ng/kg</td>
</tr>
</tbody>
</table>
To convert concentrations in mg/L (or ppm in dilute solution) to molarity, divide by the molar mass of the analyte to convert mass in mg into a corresponding number of moles.

What is the molarity of a 6.2 mg/L solution of O$_2$(aq)?

To convert from molarity to mg/L (or ppm in dilute solution), multiply by the molar mass of the analyte to convert moles into corresponding number of moles.

The Maximum Acceptable Concentration (MAC) of Pb in drinking water is 10 ppb. If a sample has concentration of 55 nM, does it exceed the MAC?

*Note 1*: In seawater, 1 mg/L ≠ 1 ppm since the density of seawater is 1.03 g/mL.

Hence, 1.00 mg/L$_{\text{seawater}}$ = 1.00 mg/L x 1 mL/1.03 g x 1 L/1000 mL x 1000 mg/g = 0.971 mg/kg or 0.971 ppm

*Note 2*: Some concentrations are expressed in terms the species actually measured e.g., mg/L of NO$_3^-$ (mass of nitrate ions per liter)

Or in terms of a particular element in a species that was measured. e.g., mg/L of NO$_3^-$ - N (mass of nitrogen in the form nitrate ions per liter)

To convert from one to the other of these, use the molar mass ratio of the element to that of the chemical species measured. In the example above use; 14 mg N/62 mg NO$_3^-$. It is important to clearly report unit values to avoid serious error in interpretation of results. Similar situations arise in reporting the concentrations of ammonia-nitrogen, phosphates-phosphorous and others.

*Note 3*: Some aggregate parameters are reported in terms of a single surrogate species. e.g., total hardness is usually reported as the mass of CaCO$_3$ that would be required to provide the same number of moles of calcium ions.

UNITS OF CONCENTRATION
Normality is a somewhat dated concentration unit that is still encountered in many texts and lab manuals. It has advantages when carrying out titration calculations, however it can be confusing for the uninitiated. Normality is defined as the number of equivalents of solute per liter, and as such, is similar to Molarity.

\[
\text{# equivalents of solute} = \text{mass of solute/ equiv. weight}
\]

where the Equiv. Weight = M.W./K

(i.e., the equivalent weight is some fraction of the molecular weight)

where \( K = \# \text{equivalents per mole} \), \( K \) is an integer constant \( \geq 1 \)

Hence, \( N = K \times M \)

(i.e., normalities are always equal to or greater than molarities)

\( K \) for a particular species is defined by the reaction type and the balanced chemical reaction.

For acid/base rxn’s: \( K \) is the number of moles of \( \text{H}^+ \) ions produced or neutralized per mole of acid or base supplied. Thus,

<table>
<thead>
<tr>
<th>Acid/base</th>
<th>( K )</th>
<th>M.W.</th>
<th>E.W.</th>
</tr>
</thead>
<tbody>
<tr>
<td>HCl</td>
<td>1</td>
<td>36.5</td>
<td>36.5</td>
</tr>
<tr>
<td>( \text{H}_2\text{SO}_4 )</td>
<td>2</td>
<td>98.1</td>
<td>49.0</td>
</tr>
<tr>
<td>( \text{CaCO}_3 )</td>
<td>2</td>
<td>100</td>
<td>50.0</td>
</tr>
<tr>
<td>( \text{Al(OH)}_3 )</td>
<td>3</td>
<td>78.0</td>
<td>26.0</td>
</tr>
</tbody>
</table>

For oxidation/reduction reactions, \( K \) is the number of moles of e- transferred per mole of oxidant or reductant in the balanced half-reaction.

<table>
<thead>
<tr>
<th>Balanced half reaction</th>
<th>( K )</th>
</tr>
</thead>
<tbody>
<tr>
<td>( \text{Fe}^{3+} \rightarrow \text{Fe} )</td>
<td>3</td>
</tr>
<tr>
<td>( \text{I}_2 \rightarrow 2 \text{I}^- )</td>
<td>2</td>
</tr>
<tr>
<td>( 2 \text{S}_2\text{O}_3^{2-} \rightarrow \text{S}_4\text{O}_6^{2-} )</td>
<td>1</td>
</tr>
</tbody>
</table>

Using Normality in titration calculations.

Method 1: use the appropriate value of \( K \) to convert Molarity, (i.e., \( 0.250 \text{ N \text{H}_2\text{SO}_4} = 0.125 \text{ M \text{H}_2\text{SO}_4} \)) and use the coefficients in the balanced chemical equations to solve for the number of moles of analyte in given sample volume.

Method 2: use the normal concentrations directly ignoring the coefficients in the balanced chemical equation.

\( \# \text{ of equiv. of analyte} = \# \text{ equiv. titrant} \)

The number of equiv. of analyte in a given volume of sample can now be converted to moles/L or mg/L using \( K \) or E.W., respectively.
More on those darn Normalities

Normality (N) is an expression of solute concentration like Molarity (M), except that it takes into account the actual number of reacting species per mole of reagent (i.e., protons in the case of acid/base reactions or electrons in the case of redox reactions). For acids, an equivalent is defined as one mole of protons. The equivalent amount of any acid is the amount of acid that delivers one mole of $H^+$. So for $H_2SO_4$, one equivalent is $\frac{1}{2}$ of one mole, since each mole of $H_2SO_4$ produces two moles of $H^+$. Consequently, the equivalent weight is half of the molecular weight. Similarly, for bases an equivalent amount of a base is defined as the amount of base that neutralizes one mole of $H^+$. For $CaCO_3$, one equivalent is $\frac{1}{2}$ of one mole, since each mole of $CaCO_3$ neutralizes two moles of $H^+$. And again, the equivalent weight is $\frac{1}{2}$ the molecular weight.

Put another way, $K$ (which is an expression of the number of equivalents supplied per mole of a substance) is equal to the number of moles of $H^+$ produced per mole of substance. Thus, $K = 1$ equiv/mole for $HCl$ and $NaOH$, but $K = 2$ equiv/mole for $H_2SO_4$ and $CaCO_3$.

For redox rxns, an equivalent is defined as the amount of a substance that delivers one mole of electrons. So for the reaction in which

$$O_2 \rightarrow 2 H_2O$$

The oxidation state of each oxygen atom drops from 0 to $-2$. Thus a total of 4 equivalents have been transferred for each mole of $O_2$ reacted and $K = 4$ equiv/mole.

Put another way, $K$ (which is an expression of the number of equivalents supplied per mole of a substance) is equal to the number of moles of $e^-$ produced per mole of substance. For the reaction

$$2 S_2O_3^{2-} \rightarrow S_4O_6^{2-}$$

The oxidation state on each sulfur increases from 2 to 2.5 (on average) for a net change of $\frac{1}{2}$ per $S$ atom. Since there are two $S$ atoms per $S_2O_3^{2-}$, each mole of thiosulfate is involved in the transfer of 1 equivalent of $e^-$ in reacting to form $S_4O_6^{2-}$. Thus $K = 1$.

<table>
<thead>
<tr>
<th>Conversion Chart for Concentrations of $O_2$</th>
</tr>
</thead>
<tbody>
<tr>
<td><strong>FROM</strong></td>
</tr>
<tr>
<td>-----------</td>
</tr>
<tr>
<td>mg $O_2$ /L</td>
</tr>
<tr>
<td>moles $O_2$ /L</td>
</tr>
<tr>
<td>equiv $O_2$ /L</td>
</tr>
</tbody>
</table>

Construct a similar conversion table for $CaCO_3$. Other conversion charts can be prepared that include converting to mg/L $NO_3^- - N$, mg/L $NO_3^-$ and mM.

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