

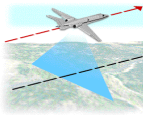
# FRST121 Maps & Photos



## Air photo geometry and scale



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Bill Beese

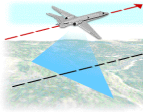


## Outline

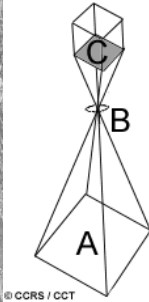


1. How photos and maps differ
2. Geometry: similar triangles
3. Scale: ratios, variation
4. Examples

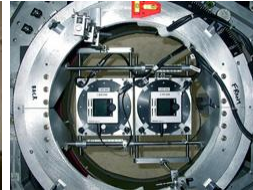




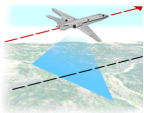
# Aerial photo equipment



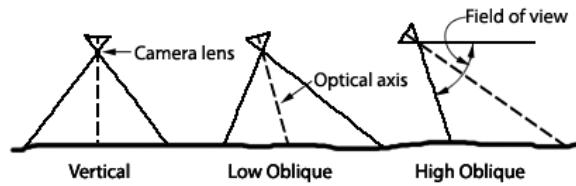
© CCRS / CCT



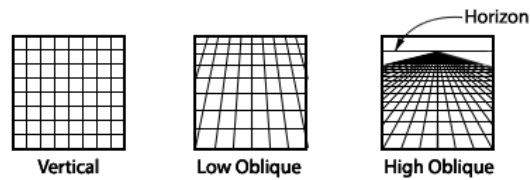
Images from Selkirk Remote Sensing



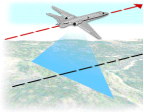
# Photos: different perspectives



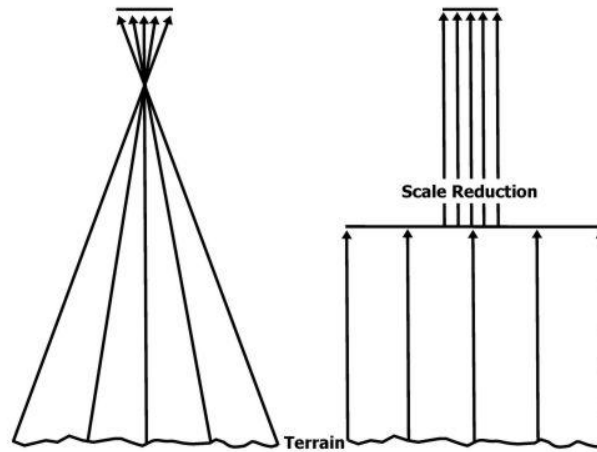
Camera orientation for various types of aerial photographs



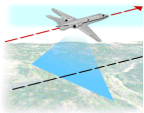
How a grid of section lines appears on various types of photos.



## How aerial photos and maps differ



Perspective vs orthographic projection

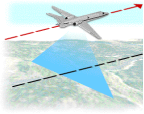


## Except...Ortho-photos

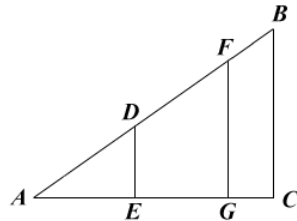


A photo-map made from images that have been corrected for distortion and digitally 'glued' together





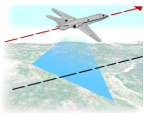
## Geometry: similar triangles



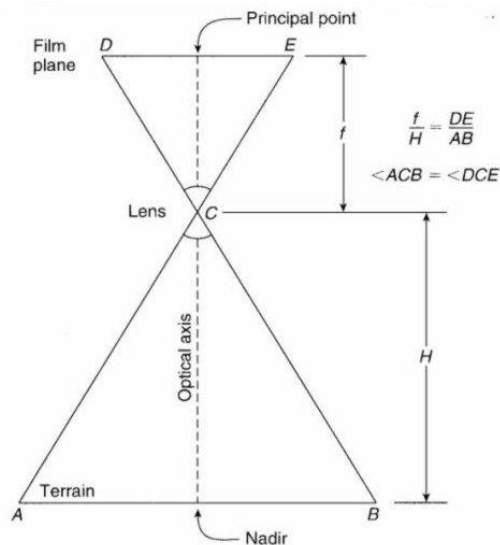
$$\frac{AB}{AC} = \frac{AD}{AE}$$

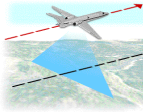
"Similar" if respective angles are equal.  
 Example:  $ABC$ ,  $ADE$  and  $AFG$  are similar

So...  
 ratios of the lengths of corresponding sides are equal.



## Geometry: similar triangles





## Scale calculation

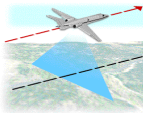
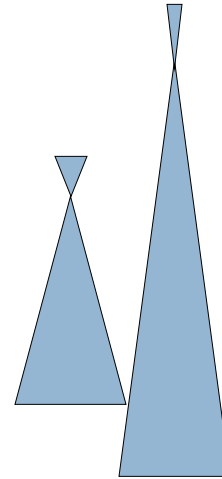


$$\frac{\text{PD Photo Distance}}{\text{GD Ground Distance}} = \frac{1}{X}$$

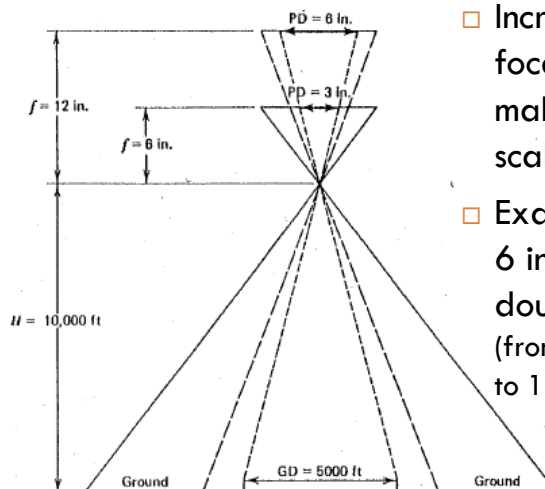
$$\frac{f \text{ focal distance}}{H \text{ Ht above ground}} = \frac{1}{X}$$

**Scale varies with both  
f and H**

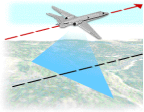
**(distance from lens)**



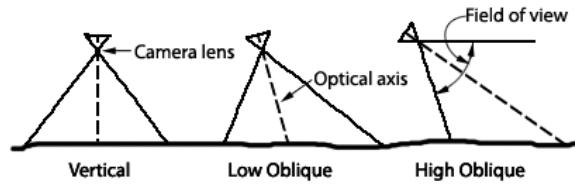
## Effect of focal length on scale



- Increasing the focal length makes the scale larger
- Example:  
6 in to 12 in  
doubles scale  
(from 1:20000  
to 1:10000)



## Scale also varies with tilt

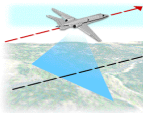


Camera orientation for various types of aerial photographs



How a grid of section lines appears on various types of photos.

Can ignore if  $< 3$  degrees



## Scale changes with relief

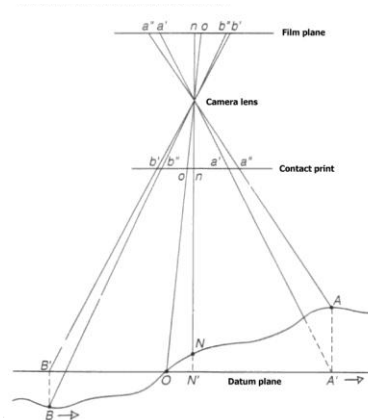


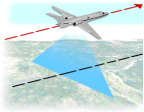
Scale at point A  
will be different than B

How?  $A > B$

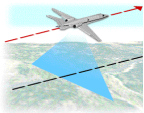
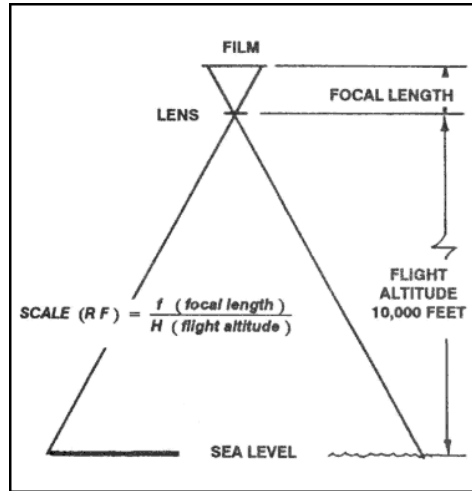
(higher elevation areas  
will appear larger on  
the photo)

Average photo elevation  
vs. point elevations





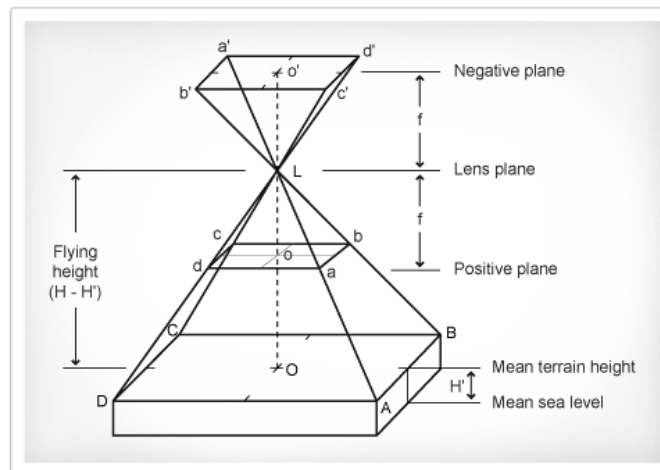
## Simple at the seashore

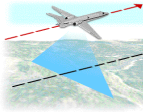


## Adjust "H" for terrain height



$H = \text{Altitude (of camera lens)} - \text{Elevation (ground)}$





## Example scale calculations



- What if the distance on a photo between two points is 10cm, and the ground distance is 1000m. What is the scale?

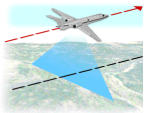
$$10\text{cm} / 1000\text{m} \times 100\text{cm (per m)} = 1:10,000$$

- What if the focal distance (f) for a photo is 6 inches, and the scale is 1:15,000. How high was the plane flying (in feet)?

$$f/H = 1/15000 \text{ So... } 0.5 \text{ ft} / H \text{ ft} = 1/15000$$

$$15000 \times 0.5 = 7500 \text{ ft (if we're talking sea level)}$$

If the ground elevation was 2000 ft, then how would we figure this out??



## Example scale calculations



- What if the focal distance (f) for a photo is 6 inches, and the scale is 1:15,000, and the ground elevation is 2,000 ft. How high was the plane flying (in feet)?

First,  $H = \text{Flying Altitude} - \text{Elevation}$

So...  $H = \text{Alt} - 2000 \text{ ft, or}$

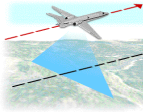
$$H + 2000 = \text{Altitude}$$

$$f/H = 1/15000 \text{ So... } 0.5 \text{ ft} / H \text{ ft} = 1/15000$$

$$15000 \times 0.5 = 7500 \text{ ft (same H as before)}$$

$$7500 + 2000 = 9500 \text{ ft (Altitude of the plane)}$$





## Example scale calculations



- What if we know the flying altitude (23,000 ft), the focal length (305mm) and the photo scale (1:20000). How would we get the avg elevation of the photo in meters?

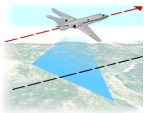
First,  $f/H = 1/20000$  So...  $30.5\text{cm} / H\text{ cm} = 1/20000$   
 $20000 \times 30.5 = 610,000\text{ cm} / 2.54\text{cm/in} / 12\text{in/ft} = 20,013\text{ ft}$

Next,  $H = \text{Flying Altitude} - \text{Elevation}$

So...  $H = 23000 - \text{Elev (ft)}$

So...  $20,013 = 23,000 - \text{Elev (ft)}$

That's  $2987\text{ ft} / 3.28\text{ ft/m} = 911\text{m}$



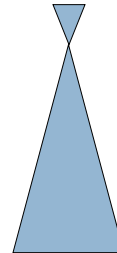
## All you need to know is...



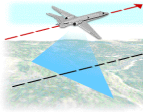
**1**  $\frac{\text{PD Photo Distance}}{\text{GD Ground Distance}} = \frac{1}{x}$

**2**  $\frac{f \text{ focal distance}}{H \text{ Ht above ground}} = \frac{1}{x}$

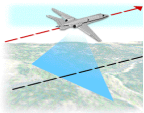
**3**  $H = \text{Altitude (of camera lens)} - \text{Elevation (ground)}$



**Remember: same units!**



## A scale we won't be talking about



## Another example...



$$\text{SCALE (RF)} = \frac{f \text{ (focal length)}}{H \text{ (flight altitude)} - h \text{ (average ground elevation)}}$$

**Example:**  
 $f = 6 \text{ inches}$  or  $15.2 \text{ centimeters}$   
 $H = 10,000 \text{ feet}$  or  $3,048 \text{ meters}$   
 $f = 850 \text{ feet}$  or  $259.08 \text{ meters}$

**With metric measures:**  

$$\frac{15.2}{(3,048 - 259.08) \times 100} = \frac{15.2}{278,900} = \frac{1}{18,300} \text{ (approximately)}$$
 or 1:18,300

**With English measurements:**  

$$\frac{0.5}{10,000 \text{ feet} - 850 \text{ feet}} = \frac{0.5}{9150} = \frac{1}{18,300}$$
 or 1:18,300

The diagram shows a camera's optical system. A lens is positioned at a focal length of 6 inches from a film plane. The camera is flying at an altitude of 10,000 feet above the ground. The ground level is labeled as sea level, and the average terrain elevation is 850 feet. The diagram illustrates the geometry of the camera's field of view and how it relates to the scale of the resulting image.